## EUREMASS

A Story of Units

## Pleasanton Mathematics Curriculum

## Grade 5 • MODULE 6

## Problem Solving with the Coordinate Plane

## PROBLem SeTS

Video tutorials: http://embarc.online Info for parents: http://bit.ly/pusdmath

# 5 Mathematics Curriculum 

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Answer Key ..... 450 accurate measurements. Adjust copier or printer settings to actual size and set page scaling to none.

Name $\qquad$ Date $\qquad$

1. Each shape was placed at a point on the number line $\boldsymbol{s}$. Give the coordinate of each point below.
a. $\qquad$
b.

c.

d. $\qquad$

2. Plot the points on the number lines.


3. Number line $\boldsymbol{g}$ is labeled from 0 to 6 . Use number line $\boldsymbol{g}$ below to answer the questions.

a. Plot point $A$ at $\frac{3}{4}$.
b. Label a point that lies at $4 \frac{1}{2}$ as $B$.
c. Label a point, $C$, whose distance from zero is 5 more than that of $A$. The coordinate of $C$ is $\qquad$ -
d. Plot a point, $D$, whose distance from zero is $1 \frac{1}{4}$ less than that of $B$. The coordinate of $D$ is $\qquad$ .
e. The distance of $E$ from zero is $1 \frac{3}{4}$ more than that of $D$. Plot point $E$.
f. What is the coordinate of the point that lies halfway between $A$ and $D$ ? $\qquad$ Label this point $F$.
4. Mrs. Fan asked her fifth-grade class to create a number line. Lenox created the number line below:


Parks said Lenox's number line is wrong because numbers should always increase from left to right. Who is correct? Explain your thinking.
5. A pirate marked the palm tree on his treasure map and buried his treasure 30 feet away. Do you think he will be able to easily find his treasure when he returns? Why or why not? What might he do to make it easier to find?


Name $\qquad$ Date $\qquad$
1.
a. Use a set square to draw a line perpendicular to the $x$-axes through points $P, Q$, and $R$. Label the new line as the $y$-axis.

a. Choose one of the sets of perpendicular lines above, and create a coordinate plane. Mark 7 units on each axis, and label them as whole numbers.
2. Use the coordinate plane to answer the following.

a. Name the shape at each location.

| $x$-coordinate | $y$-coordinate | Shape |
| :---: | :---: | :---: |
| 2 | 5 |  |
| 1 | 2 |  |
| 5 | 6 |  |
| 6 | 5 |  |

b. Which shape is 2 units from the $y$-axis?
c. Which shape has an $x$-coordinate of 0 ?
d. Which shape is 4 units from the $y$-axis and 3 units from the $x$-axis?
3. Use the coordinate plane to answer the following.

b. Name the shape whose $x$-coordinate is $\frac{1}{2}$ more than the value of the heart's $x$-coordinate.
c. Plot a triangle at $(3,4)$.
d. Plot a square at $\left(4 \frac{3}{4}, 5\right)$.
e. Plot an $X$ at $\left(\frac{1}{2}, \frac{3}{4}\right)$.
4. The pirate's treasure is buried at the $\mathbf{X}$ on the map. How could a coordinate plane make describing its location easier?

$\qquad$ Date $\qquad$

1. Use the grid below to complete the following tasks.
a. Construct an $x$-axis that passes through points $A$ and $B$.
b. Construct a perpendicular $y$-axis that passes through points $C$ and $F$.
c. Label the origin as 0 .
d. The $x$-coordinate of $B$ is $5 \frac{2}{3}$. Label the whole numbers along the $x$-axis.
e. The $y$-coordinate of $C$ is $5 \frac{1}{3}$. Label the whole numbers along the $y$-axis.

2. For all of the following problems, consider the points $A$ through $N$ on the previous page.
a. Identify all of the points that have an $x$-coordinate of $3 \frac{1}{3}$.
b. Identify all of the points that have a $y$-coordinate of $2 \frac{2}{3}$.
c. Which point is $3 \frac{1}{3}$ units above the $x$-axis and $2 \frac{2}{3}$ units to the right of the $y$-axis? Name the point, and give its coordinate pair.
d. Which point is located $5 \frac{1}{3}$ units from the $y$-axis?
e. Which point is located $1 \frac{2}{3}$ units along the $x$-axis?
f. Give the coordinate pair for each of the following points.
$K$ : $\qquad$
I: $\qquad$
$B$ : $\qquad$
$C$ : $\qquad$
g. Name the points located at the following coordinates.
$\left(1 \frac{2}{3}, \frac{2}{3}\right)$ $\qquad$ (0, $2 \frac{2}{3}$ ) $\qquad$
$(1,0)$ $\qquad$
$\left(2,5 \frac{2}{3}\right)$ $\qquad$
h. Which point has an equal $x$ - and $y$-coordinate? $\qquad$
i. Give the coordinates for the intersection of the two axes. $\qquad$ , $\qquad$ ) Another name for this point on the plane is the $\qquad$ -.
j. Plot the following points.
$P:\left(4 \frac{1}{3}, 4\right)$
$Q:\left(\frac{1}{3}, 6\right)$
$R:\left(4 \frac{2}{3}, 1\right)$
$S:\left(0,1 \frac{2}{3}\right)$
k. What is the distance between $E$ and $H$, or $E H$ ?
I. What is the length of $H D$ ?
m . Would the length of $E D$ be greater or less than $E H+H D$ ?
n. Jack was absent when the teacher explained how to describe the location of a point on the coordinate plane. Explain it to him using point $J$.

[^0]
## Battleship Rules

Goal: To sink all of your opponent's ships by correctly guessing their coordinates.

## Materials

- 1 grid sheet (per person/per game)
- Red crayon/marker for hits
- Black crayon/marker for misses
- Folder to place between players


## Ships

- Each player must mark 5 ships on the grid.
- Aircraft carrier—plot 5 points.
- Battleship-plot 4 points.
- Cruiser-plot 3 points.
- Submarine-plot 3 points.
- Patrol boat-plot 2 points.


## Setup

- With your opponent, choose a unit length and fractional unit for the coordinate plane.
- Label the chosen units on both grid sheets.
- Secretly select locations for each of the 5 ships on your My Ships grid.
- All ships must be placed horizontally or vertically on the coordinate plane.
- Ships can touch each other, but they may not occupy the same coordinate.


## Play

- Players take turns firing one shot to attack enemy ships.
- On your turn, call out the coordinates of your attacking shot. Record the coordinates of each attack shot.
- Your opponent checks his/her My Ships grid. If that coordinate is unoccupied, your opponent says, "Miss." If you named a coordinate occupied by a ship, your opponent says, "Hit."
- Mark each attempted shot on your Enemy Ships grid. Mark a black $\boldsymbol{*}$ on the coordinate if your opponent says, "Miss." Mark a red $\checkmark$ on the coordinate if your opponent says, "Hit."
- On your opponent's turn, if he/she hits one of your ships, mark a red $\checkmark$ on that coordinate of your My Ships grid. When one of your ships has every coordinate marked with a $\checkmark$, say, "You've sunk my [name of ship]."


## Victory

- The first player to sink all (or the most) opposing ships, wins.


## My Ships

- Draw a red $\checkmark$ over any coordinate your opponent hits.
- Once all of the coordinates of any ship have been hit, say, "You've sunk my [name of ship]."


Aircraft carrier-5 points Battleship-4 points Cruiser-3 points
Submarine-3 points
Patrol boat-2 points

## Enemy Ships

- Draw a black $\boldsymbol{*}$ on the coordinate if your opponent says, "Miss."


## Attack Shots

- Record the coordinates of each shot below and whether it was a $\boldsymbol{\checkmark}$ (hit) or an (miss).
$\qquad$ , $\qquad$ ) $\qquad$ , $\qquad$ )
$\qquad$ , $\qquad$ -
( $\qquad$ , $\qquad$
$\qquad$ , ) $\qquad$ _, $\qquad$ )
$\qquad$
$\qquad$ -)
1 $\qquad$ , ___ )
$\qquad$ , ___ ) )
$\qquad$ , ___ ) 1 $\qquad$ , $\qquad$ _) )
1 $\qquad$ , $\qquad$ )
$\qquad$ , $\qquad$ ) ( $\qquad$ , $\qquad$ )
$\qquad$ , ___ ) ) $\qquad$ , $\qquad$ )
- Draw a red $\checkmark$ on the coordinate if your opponent says, "Hit."
- Draw a circle around the coordinates of a sunken ship.

Name $\qquad$ Date $\qquad$

1. Use the coordinate plane to the right to answer the following questions.
a. Use a straightedge to construct a line that goes through points $A$ and $B$. Label the line $e$.
b. Line $e$ is parallel to the $\qquad$ -axis and is perpendicular to the $\qquad$ -axis.
c. Plot two more points on line $e$. Name them $C$ and $D$.
d. Give the coordinates of each point below.
A: $\qquad$

B: $\qquad$

$C$ : $\qquad$ D: $\qquad$
e. What do all of the points of line $e$ have in common?
f. Give the coordinates of another point that would fall on line $e$ with an $x$-coordinate greater than 15 .
2. Plot the following points on the coordinate plane to the right.
$P:\left(1 \frac{1}{2}, \frac{1}{2}\right) Q:\left(1 \frac{1}{2}, 2 \frac{1}{2}\right)$
$R:\left(1 \frac{1}{2}, 1 \frac{1}{4}\right)$
$S:\left(1 \frac{1}{2}, \frac{3}{4}\right)$
a. Use a straightedge to draw a line to connect these points. Label the line $h$.
b. In line $h, x=$ $\qquad$ for all values of $y$.
c. Circle the correct word.


Line $h$ is parallel perpendicular to the $x$-axis.

Line $h$ is parallel perpendicular to the $y$-axis.
d. What pattern occurs in the coordinate pairs that let you know that line $h$ is vertical?
3. For each pair of points below, think about the line that joins them. For which pairs is the line parallel to the $x$-axis? Circle your answer(s). Without plotting them, explain how you know.
a. $(1.4,2.2)$ and $(4.1,2.4)$
b. $(3,9)$ and $(8,9)$
c. $\left(1 \frac{1}{4}, 2\right)$ and $\left(1 \frac{1}{4}, 8\right)$
4. For each pair of points below, think about the line that joins them. For which pairs is the line parallel to the $y$-axis? Circle your answer(s). Then, give 2 other coordinate pairs that would also fall on this line.
a. $(4,12)$ and $(6,12)$
b. $\left(\frac{3}{5}, 2 \frac{3}{5}\right)$ and $\left(\frac{1}{5}, 3 \frac{1}{5}\right)$
c. $(0.8,1.9)$ and $(0.8,2.3)$
5. Write the coordinate pairs of 3 points that can be connected to construct a line that is $5 \frac{1}{2}$ units to the right of and parallel to the $y$-axis.
a.
b. $\qquad$ c. $\qquad$
6. Write the coordinate pairs of 3 points that lie on the $x$-axis.
a. $\qquad$
b. $\qquad$
c. $\qquad$
7. Adam and Janice are playing Battleship. Presented in the table is a record of Adam's guesses so far.
He has hit Janice's battleship using these coordinate pairs. What should he guess next? How do you know? Explain using words and pictures.
$(3,11) \quad$ hit
$(2,11) \quad$ miss
$(3,10)$ hit
$(4,11) \quad$ miss
$(3,9) \quad$ miss

| Point | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $H$ |  |  |  |
| $\boldsymbol{I}$ |  |  |  |
| $J$ |  |  |  |
| $K$ |  |  |  |
| $L$ |  |  |  |


b.


| Point | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{D}$ | $2 \frac{1}{2}$ | 0 | $\left(2 \frac{1}{2}, 0\right)$ |
| $\boldsymbol{E}$ | $2 \frac{1}{2}$ | 2 | $\left(2 \frac{1}{2}, 2\right)$ |
| $\boldsymbol{F}$ | $2 \frac{1}{2}$ | 4 | $\left(2 \frac{1}{2}, 4\right)$ |

coordinate plane practice

Name $\qquad$ Date $\qquad$

1. Plot the following points, and label them on the coordinate plane.
$A:(0.3,0.1) \quad B:(0.3,0.7)$
$C:(0.2,0.9) \quad D:(0.4,0.9)$
a. Use a straightedge to construct line segments $\overline{A B}$ and $\overline{C D}$.
b. Line segment $\qquad$ is parallel to the $x$ axis and is perpendicular to the $y$-axis.
c. Line segment $\qquad$ is parallel to the $y$ axis and is perpendicular to the $x$-axis.

d. Plot a point on line segment $\overline{A B}$ that is not at the endpoints, and name it $U$. Write the coordinates. U( $\qquad$ , $\qquad$ )
e. Plot a point on line segment $\overline{C D}$, and name it $V$. Write the coordinates. $V$ ( $\qquad$ , $\qquad$ )
2. Construct line $f$ such that the $y$-coordinate of every point is $3 \frac{1}{2}$, and construct line $g$ such that the $x$-coordinate of every point is $4 \frac{1}{2}$.
a. Line $f$ is $\qquad$ units from the $x$-axis.
b. Give the coordinates of the point on line $f$ that is $\frac{1}{2}$ unit from the $y$-axis. $\qquad$
c. With a blue pencil, shade the portion of the grid that is less than $3 \frac{1}{2}$ units from the $x$-axis.
d. Line $g$ is $\qquad$ units from the $y$-axis.
e. Give the coordinates of the point on line $g$ that is 5 units from the $x$-axis. $\qquad$

f. With a red pencil, shade the portion of the grid that is more than $4 \frac{1}{2}$ units from the $y$ axis.
3. Complete the following tasks on the plane below.
a. Construct a line $m$ that is perpendicular to the $x$-axis and 3.2 units from the $y$-axis.
b. Construct a line $a$ that is 0.8 unit from the $x$-axis.
c. Construct a line $t$ that is parallel to line $m$ and is halfway between line $m$ and the $y$-axis.
d. Construct a line $h$ that is perpendicular to line $t$ and passes through the point (1.2, 2.4).
e. Using a blue pencil, shade the region that contains points that are more than 1.6 units and less than 3.2 units from the $y$-axis.
f. Using a red pencil, shade the region that contains points that are more than 0.8 unit and less than 2.4 units from the $x$-axis.
g. Give the coordinates of a point that lies in the double-shaded region.


Name $\qquad$ Date $\qquad$

1. Complete the chart. Then, plot the points on the coordinate plane below.

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
| 0 | 1 | $(0,1)$ |
| 2 | 3 |  |
| 4 | 5 |  |
| 6 | 7 |  |

a. Use a straightedge to draw a line connecting these points.

b. Write a rule showing the relationship between the $x$ - and $y$-coordinates of points on the line.
c. Name 2 other points that are on this line. $\qquad$
$\qquad$
2. Complete the chart. Then, plot the points on the coordinate plane below.

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
| $\frac{1}{2}$ | 1 |  |
| 1 | 2 |  |
| $1 \frac{1}{2}$ | 3 |  |
| 2 | 4 |  |

a. Use a straightedge to draw a line connecting these points.

b. Write a rule showing the relationship between the $x$ - and $y$-coordinates.
c. Name 2 other points that are on this line. $\qquad$
$\qquad$
3. Use the coordinate plane below to answer the following questions.

a. Give the coordinates for 3 points that are on line $a$. $\qquad$
b. Write a rule that describes the relationship between the $x$ - and $y$-coordinates for the points on line $a$.
c. What do you notice about the $y$-coordinates of every point on line $b$ ?
d. Fill in the missing coordinates for points on line $d$.
(12, $\qquad$ $(6, \ldots \quad$ ) $\qquad$ ,24)
(28, $\qquad$
$\qquad$ 28)
e. For any point on line $c$, the $x$-coordinate is $\qquad$ .
f. Each of the points lies on at least 1 of the lines shown in the plane on the previous page. Identify a line that contains each of the following points.
i. $(7,7) \_a$
ii. $(14,8)$ $\qquad$
iii. $(5,10)$ $\qquad$
iv. $(0,17)$ $\qquad$
v. $(15.3,9.3)$ $\qquad$ vi. $(20,40)$

Name $\qquad$ Date $\qquad$

1. Create a table of 3 values for $x$ and $y$ such that each $y$-coordinate is 3 more than the corresponding $x$-coordinate.

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
|  |  |  |
|  |  |  |
|  |  |  |

a. Plot each point on the coordinate plane.
b. Use a straightedge to draw a line connecting these points.

c. Give the coordinates of 2 other points that fall on this line with $x$-coordinates greater than 12 .
$\qquad$
$\qquad$ ) and ( $\qquad$ , _
2. Create a table of 3 values for $x$ and $y$ such that each $y$-coordinate is 3 times as much as its corresponding $x$-coordinate.

| $x$ | $y$ | $(x, y)$ |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |

a. Plot each point on the coordinate plane.
b. Use a straightedge to draw a line connecting these points.

c. Give the coordinates of 2 other points that fall on this line with $y$-coordinates greater than 25 .
$\qquad$ , $\qquad$ ) and ( $\qquad$ , _
3. Create a table of 5 values for $x$ and $y$ such that each $y$-coordinate is 1 more than 3 times as much as its corresponding $x$ value.

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |


a. Plot each point on the coordinate plane.
b. Use a straightedge to draw a line connecting these points.
c. Give the coordinates of 2 other points that would fall on this line whose $x$-coordinates are greater than 12.
$\qquad$
4. Use the coordinate plane below to complete the following tasks.
a. Graph the lines on the plane.
line $\ell$ : $x$ is equal to $y$

|  | $x$ | $y$ | $(x, y)$ |
| :--- | :--- | :--- | :--- |
| $A$ |  |  |  |
| $B$ |  |  |  |
| $C$ |  |  |  |

line $m: y$ is 1 more than $x$

|  | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $G$ |  |  |  |
| $H$ |  |  |  |
| $I$ |  |  |  |

line $n: y$ is 1 more than twice $x$

|  | $x$ | $y$ | $(x, y)$ |
| :---: | :--- | :--- | :--- |
| $S$ |  |  |  |
| $T$ |  |  |  |
| $U$ |  |  |  |


b. Which two lines intersect? Give the coordinates of their intersection.
c. Which two lines are parallel?
d. Give the rule for another line that would be parallel to the lines you listed in Problem 4(c).

Name $\qquad$ Date $\qquad$

1. Complete the table for the given rules.

Line $a$

Rule: $y$ is 1 more than $x$

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
| 1 |  |  |
| 5 |  |  |
| 9 |  |  |
| 13 |  |  |

Line $b$

Rule: $y$ is 4 more than $x$

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
| 0 |  |  |
| 5 |  |  |
| 8 |  |  |
| 11 |  |  |


a. Construct each line on the coordinate plane above.
b. Compare and contrast these lines.
c. Based on the patterns you see, predict what line $c$, whose rule is $y$ is 7 more than $x$, would look like. Draw your prediction on the plane above.
2. Complete the table for the given rules.

$$
\text { Line } e
$$

Rule: $y$ is twice as much as $x$

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
| 0 |  |  |
| 2 |  |  |
| 5 |  |  |
| 9 |  |  |

Line $f$
Rule: $y$ is half as much as $x$

| $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: |
| 0 |  |  |
| 6 |  |  |
| 10 |  |  |
| 20 |  |  |


a. Construct each line on the coordinate plane above.
b. Compare and contrast these lines.
c. Based on the patterns you see, predict what line $g$, whose rule is $y$ is 4 times as much as $x$, would look like. Draw your prediction in the plane above.

Name $\qquad$ Date $\qquad$

1. Use the coordinate plane below to complete the following tasks.
a. Line $p$ represents the rule $x$ and $y$ are equal.
b. Construct a line, $d$, that is parallel to line $p$ and contains point $D$.
c. Name 3 coordinate pairs on line $d$.
d. Identify a rule to describe line $d$.
e. Construct a line, $e$, that is parallel to line $p$ and contains point $E$.
f. Name 3 points on line $e$.
g. Identify a rule to describe line $e$.

h. Compare and contrast lines $d$ and $e$ in terms of their relationship to line $p$.
2. Write a rule for a fourth line that would be parallel to those above and would contain the point $\left(3 \frac{1}{2}, 6\right)$. Explain how you know.
3. Use the coordinate plane below to complete the following tasks.
a. Line $p$ represents the rule $x$ and $y$ are equal.
b. Construct a line, $v$, that contains the origin and point $V$.
c. Name 3 points on line $v$.
d. Identify a rule to describe line $v$.
e. Construct a line, w, that contains the origin and point $W$.
f. Name 3 points on line $w$.
g. Identify a rule to describe line $w$.

h. Compare and contrast lines $v$ and $w$ in terms of their relationship to line $p$.
i. What patterns do you see in lines that are generated by multiplication rules?
4. Circle the rules that generate lines that are parallel to each other.
add 5 to $x$
multiply $x$ by $\frac{2}{3}$
$x$ plus $\frac{1}{2}$
$x$ times $1 \frac{1}{2}$

Name $\qquad$ Date $\qquad$

1. Complete the tables for the given rules.

Line $l$
Rule: Double $x$

| $x$ | $y$ | $(x, y)$ |
| :--- | :--- | :--- |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |

Line $m$
Rule: Double $x$, and then
add 1

| $x$ | $y$ | $(x, y)$ |
| :--- | :--- | :--- |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |


a. Draw each line on the coordinate plane above.
b. Compare and contrast these lines.
c. Based on the patterns you see, predict what the line for the rule double $x$, and then subtract 1 would look like. Draw the line on the plane above.
2. Circle the point(s) that the line for the rule multiply $x$ by $\frac{1}{3^{\prime}}$ and then add 1 would contain.
( $0, \frac{1}{3}$ )
$\left(2,1 \frac{2}{3}\right)$
( $1 \frac{1}{2}, 1 \frac{1}{2}$ )
( $2 \frac{1}{4}, 2 \frac{1}{4}$ )
a. Explain how you know.
b. Give two other points that fall on this line.
3. Complete the tables for the given rules.

Line $\ell$
Rule: Halve $x$

| $x$ | $y$ | $(x, y)$ |
| :--- | :--- | :--- |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |

Line $m$
Rule: Halve $x$, and then
add $1 \frac{1}{2}$

| $x$ | $y$ | $(x, y)$ |
| :--- | :--- | :--- |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |


a. Draw each line on the coordinate plane above.
b. Compare and contrast these lines.
c. Based on the patterns you see, predict what the line for the rule halve $x$, and then subtract 1 would look like. Draw the line on the plane above.
4. Circle the point(s) that the line for the rule multiply $x$ by $\frac{2}{3}$, and then subtract 1 would contain.
( $1 \frac{1}{3}, \frac{1}{9}$ )
$\left(2, \frac{1}{3}\right)$
$\left(1 \frac{3}{2}, 1 \frac{1}{2}\right)$
$(3,1)$
a. Explain how you know.
b. Give two other points that fall on this line.

Name $\qquad$ Date $\qquad$

1. Write a rule for the line that contains the points $\left(0, \frac{3}{4}\right)$ and $\left(2 \frac{1}{2}, 3 \frac{1}{4}\right)$.
a. Identify 2 more points on this line. Draw the line on the grid below.

| Point | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $B$ |  |  |  |
| $C$ |  |  |  |

b. Write a rule for a line that is parallel to $\overleftrightarrow{B C}$ and goes through point $\left(1, \frac{1}{4}\right)$.
2. Create a rule for the line that contains the points $\left(1, \frac{1}{4}\right)$ and $\left(3, \frac{3}{4}\right)$.
a. Identify 2 more points on this line. Draw the line on the grid on the right.

| Point | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $G$ |  |  |  |
| $H$ |  |  |  |


b. Write a rule for a line that passes through the origin and lies between $\overleftrightarrow{B C}$ and $\overleftrightarrow{G H}$.
3. Create a rule for a line that contains the point $\left(\frac{1}{4}, 1 \frac{1}{4}\right)$ using the operation or description below. Then, name 2 other points that would fall on each line.
a. Addition: $\qquad$

| Point | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $T$ |  |  |  |
| $U$ |  |  |  |

c. Multiplication: $\qquad$

| Point | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $A$ |  |  |  |
| $B$ |  |  |  |

d. A line parallel to the $y$-axis: $\qquad$

| Point | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $V$ |  |  |  |
| $W$ |  |  |  |

e. Multiplication with addition: $\qquad$

| Point | $\boldsymbol{x}$ | $\boldsymbol{y}$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $R$ |  |  |  |
| $S$ |  |  |  |

4. Mrs. Boyd asked her students to give a rule that could describe a line that contains the point $(0.6,1.8)$. Avi said the rule could be multiply $x$ by 3 . Ezra claims this could be a vertical line, and the rule could be $x$ is always 0.6 . Erik thinks the rule could be add 1.2 to $x$. Mrs. Boyd says that all the lines they are describing could describe a line that contains the point she gave. Explain how that is possible, and draw the lines on the coordinate plane to support your response.


## Extension:

5. Create a mixed operation rule for the line that contains the points $(0,1)$ and $(1,3)$.
a. Identify 2 more points, $O$ and $P$, on this line. Draw the line on the grid.

| Point | $x$ | $y$ | $(x, y)$ |
| :---: | :---: | :---: | :---: |
| $O$ |  |  |  |
| $P$ |  |  |  |



Name $\qquad$ Date $\qquad$

1. Use a right angle template and straightedge to draw at least four sets of parallel lines in the space below.
2. Circle the segments that are parallel.

3. Use your straightedge to draw a segment parallel to each segment through the given point.

4. Draw 2 different lines parallel to line $b$.


Name $\qquad$ Date $\qquad$

1. Use the coordinate plane below to complete the following tasks.

a. Identify the locations of $P$ and $R$. $P:\left(\_\right.$, ____ $) \quad R:(\square$, ___ $)$
b. Draw $\overleftrightarrow{P R}$.
c. Plot the following coordinate pairs on the plane.
$S:(6,7)$
$T:(11,9)$
d. Draw $\overleftrightarrow{S T}$.
e. Circle the relationship between $\overleftrightarrow{P R}$ and $\overleftrightarrow{S T}$. $\overleftrightarrow{P R} \perp \overleftrightarrow{S T} \quad \overleftrightarrow{P R} \| \overleftrightarrow{S T}$
f. Give the coordinates of a pair of points, $U$ and $V$, such that $\overleftrightarrow{U V} \| \overleftrightarrow{P R}$.
$U:\left(Z_{\square}\right.$, $V:(\square \quad$, $\quad$ )
g. Draw $\overleftrightarrow{U V}$.
2. Use the coordinate plane below to complete the following tasks.

a. Identify the locations of $E$ and $F$.
$E:$ $\qquad$
$\qquad$
$F:$ $\qquad$
$\qquad$
b. Draw $\overleftrightarrow{E F}$.
c. Generate coordinate pairs for $L$ and $M$, such that $\overleftrightarrow{E F} \| \overleftrightarrow{L M}$.

$$
L:(\ldots, \ldots) \quad M:(\ldots, \ldots)
$$

d. Draw $\overleftrightarrow{L M}$.
e. Explain the pattern you made use of when generating coordinate pairs for $L$ and $M$.
f. Give the coordinates of a point, $H$, such that $\overleftrightarrow{E F} \| \overleftrightarrow{G H}$.

$$
G:\left(1 \frac{1}{2}, 4\right) \quad H:(\ldots, \ldots)
$$

g. Explain how you chose the coordinates for $H$.

Name $\qquad$ Date $\qquad$

1. Circle the pairs of segments that are perpendicular.

2. In the space below, use your right triangle templates to draw at least 3 different sets of perpendicular lines.
3. Draw a segment perpendicular to each given segment. Show your thinking by sketching triangles as needed.

4. Draw 2 different lines perpendicular to line $e$.


Name $\qquad$ Date $\qquad$

1. Use the coordinate plane below to complete the following tasks.
a. Draw $\overline{A B}$.
b. Plot point $C(0,8)$.
c. Draw $\overline{A C}$.
d. Explain how you know $\angle C A B$ is a right angle without measuring it.

e. Sean drew the picture below to find a segment perpendicular to $\overline{A B}$. Explain why Sean is correct.

2. Use the coordinate plane below to complete the following tasks.
a. Draw $\overline{Q T}$.
b. Plot point $R\left(2,6 \frac{1}{2}\right)$.
c. Draw $\overline{Q R}$.
d. Explain how you know $\angle R Q T$ is a right angle without measuring it.
e. Compare the coordinates of points $Q$ and $T$. What is the difference of the $x$-coordinates? The $y$-coordinates?

f. Compare the coordinates of points $Q$ and $R$. What is the difference of the $x$-coordinates? The $y$-coordinates?
g. What is the relationship of the differences you found in parts (e) and (f) to the triangles of which these two segments are a part?
3. $\overleftrightarrow{E F}$ contains the following points.
$E:(4,1)$
$F:(8,7)$
Give the coordinates of a pair of points $G$ and $H$, such that $\overleftrightarrow{E F} \perp \overleftrightarrow{G H}$.
$G:$ $\qquad$ ) $H:$ $\qquad$ , _)

Name $\qquad$ Date $\qquad$

1. Draw to create a figure that is symmetric about $\overleftrightarrow{A D}$.

2. Draw precisely to create a figure that is symmetric about $\overleftrightarrow{H I}$.

3. Complete the following construction in the space below.
a. Plot 3 non-collinear points, $D, E$, and $F$.
b. Draw $\overline{D E}, \overline{E F}$, and $\overleftrightarrow{D F}$.
c. Plot point $G$, and draw the remaining sides, such that quadrilateral $D E F G$ is symmetric about $\overleftrightarrow{D F}$.
$\square$
4. Stu says that quadrilateral $H I J K$ is symmetric about $\overleftrightarrow{H J}$ because $I L=L K$. Use your tools to determine Stu's mistake. Explain your thinking.


Name $\qquad$ Date $\qquad$

1. Use the plane to the right to complete the following tasks.
a. Draw a line $t$ whose rule is $y$ is always 0.7.
b. Plot the points from Table A on the grid in order. Then, draw line segments to connect the points.

Table A

| $(x, y)$ |
| :---: |
| $(0.1,0.5)$ |
| $(0.2,0.3)$ |
| $(0.3,0.5)$ |
| $(0.5,0.1)$ |
| $(0.6,0.2)$ |
| $(0.8,0.2)$ |
| $(0.9,0.1)$ |
| $(1.1,0.5)$ |
| $(1.2,0.3)$ |
| $(1.3,0.5)$ |

Table B


c. Complete the drawing to create a figure that is symmetric about line $t$. For each point in Table A, record the corresponding point on the other side of the line of symmetry in Table B.
d. Compare the $y$-coordinates in Table A with those in Table B. What do you notice?
e. Compare the $x$-coordinates in Table A with those in Table B. What do you notice?
2. This figure has a second line of symmetry. Draw the line on the plane, and write the rule for this line.
3. Use the plane below to complete the following tasks.
a. Draw a line $u$ whose rule is $y$ is equal to $x+\frac{1}{4}$.
b. Construct a figure with a total of 6 points, all on the same side of the line.
c. Record the coordinates of each point, in the order in which they were drawn, in Table A.
d. Swap your paper with a neighbor, and have her complete parts (e-f), below.

Table A

| $(x, y)$ |
| :--- |
|  |
|  |
|  |
|  |
|  |

Table B

| $(x, y)$ |
| :--- |
|  |
|  |
|  |
|  |
|  |
|  |


e. Complete the drawing to create a figure that is symmetric about $u$. For each point in Table A, record the corresponding point on the other side of the line of symmetry in Table B.
f. Explain how you found the points symmetric to your partner's about $u$.

Name $\qquad$ Date $\qquad$

1. The line graph below tracks the rain accumulation, measured every half hour, during a rainstorm that began at 2:00 p.m. and ended at 7:00 p.m. Use the information in the graph to answer the questions that follow.

a. How many inches of rain fell during this five-hour period?
b. During which half-hour period did $\frac{1}{2}$ inch of rain fall? Explain how you know.
c. During which half-hour period did rain fall most rapidly? Explain how you know.
d. Why do you think the line is horizontal between 3:30 p.m. and 4:30 p.m.?
e. For every inch of rain that fell here, a nearby community in the mountains received a foot and a half of snow. How many inches of snow fell in the mountain community between 5:00 p.m. and 7:00 p.m.?
2. Mr. Boyd checks the gauge on his home's fuel tank on the first day of every month. The line graph to the right was created using the data he collected.
a. According to the graph, during which month(s) does the amount of fuel decrease most rapidly?
b. The Boyds took a month-long vacation. During which month did this most likely occur? Explain how you know using the data in the graph.
c. Mr. Boyd's fuel company filled his tank once this year. During which month did this most likely occur? Explain how you know.

d. The Boyd family's fuel tank holds 284 gallons of fuel when full. How many gallons of fuel did the Boyds use in February?
e. Mr. Boyd pays $\$ 3.54$ per gallon of fuel. What is the cost of the fuel used in February and March?

Name $\qquad$ Date $\qquad$

1. The line graph below tracks the total tomato production for one tomato plant. The total tomato production is plotted at the end of each of 8 weeks. Use the information in the graph to answer the questions that follow.

Total Tomato Production

a. How many pounds of tomatoes did this plant produce at the end of 13 weeks?
b. How many pounds of tomatoes did this plant produce from Week 7 to Week 11? Explain how you know.
c. Which one-week period showed the greatest change in tomato production? The least? Explain how you know.
d. During Weeks 6-8, Jason fed the tomato plant just water. During Weeks 8-10, he used a mixture of water and Fertilizer A, and in Weeks 10-13, he used water and Fertilizer B on the tomato plant. Compare the tomato production for these periods of time.
2. Use the story context below to sketch a line graph. Then, answer the questions that follow.

The number of fifth-grade students attending Magnolia School has changed over time. The school opened in 2006 with 156 students in the fifth grade. The student population grew the same amount each year before reaching its largest class of 210 students in 2008. The following year, Magnolia lost oneseventh of its fifth graders. In 2010, the enrollment dropped to 154 students and remained constant in 2011. For the next two years, the enrollment grew by 7 students each year.

a. How many more fifth-grade students attended Magnolia in 2009 than in 2013?
b. Between which two consecutive years was there the greatest change in student population?
c. If the fifth-grade population continues to grow in the same pattern as in 2012 and 2013, in what year will the number of students match 2008's enrollment?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 1

## Pierre's Paper

Pierre folded a square piece of paper vertically to make two rectangles. Each rectangle had a perimeter of 39 inches. How long is each side of the original square? What is the area of the original square? What is the area of one of the rectangles?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 2

## Shopping with Elise

Elise saved \$184. She bought a scarf, a necklace, and a notebook. After her purchases, she still had \$39.50. The scarf cost three-fifths the cost of the necklace, and the notebook was one-sixth as much as the scarf. What was the cost of each item? How much more did the necklace cost than the notebook?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 3

## The Hewitt's Carpet

The Hewitt family is buying carpet for two rooms. The dining room is a square that measures 12 feet on each side. The den is 9 yards by 5 yards. Mrs. Hewitt has budgeted $\$ 2,650$ for carpeting both rooms. The green carpet she is considering costs $\$ 42.75$ per square yard, and the brown carpet's price is $\$ 4.95$ per square foot. What are the ways she can carpet the rooms and stay within her budget?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 4

AAA Taxi
AAA Taxi charges $\$ 1.75$ for the first mile and $\$ 1.05$ for each additional mile. How far could Mrs. Leslie travel for $\$ 20$ if she tips the cab driver $\$ 2.50$ ?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 5

## Pumpkins and Squash

Three pumpkins and two squash weigh 27.5 pounds. Four pumpkins and three squash weigh 37.5 pounds. Each pumpkin weighs the same as the other pumpkins, and each squash weighs the same as the other squash. How much does each pumpkin weigh? How much does each squash weigh?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 6

## Toy Cars and Trucks

Henry had 20 convertibles and 5 trucks in his miniature car collection. After Henry's aunt bought him some more miniature trucks, Henry found that one-fifth of his collection consisted of convertibles. How many trucks did his aunt buy?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 7

## Pairs of Scouts

Some girls in a Girl Scout troop are pairing up with some boys in a Boy Scout troop to practice square dancing. Two-thirds of the girls are paired with three-fifths of the boys. What fraction of the scouts are square dancing?
(Each pair is one Girl Scout and one Boy Scout. The pairs are only from these two troops.)

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 8

## Sandra's Measuring Cups

Sandra is making cookies that require $5 \frac{1}{2}$ cups of oatmeal. She has only two measuring cups: a one-half cup and a three-fourths cup. What is the smallest number of scoops that she could make in order to get $5 \frac{1}{2}$ cups?

Student $\qquad$ Team $\qquad$ Date $\qquad$ Problem 9

## Blue Squares

The dimensions of each successive blue square pictured to the right are half that of the previous blue square. The lower left blue square measures 6 inches by 6 inches.
a. Find the area of the shaded part.
b. Find the total area of the shaded and unshaded parts.
c. What fraction of the figure is shaded?


Name $\qquad$ Date $\qquad$

1. For each written phrase, write a numerical expression, and then evaluate your expression.
a. Three fifths of the sum of thirteen and six

Numerical expression:

Solution:
b. Subtract four thirds from one seventh of sixty-three.

Numerical expression:

Solution:
d. Three fourths of the product of four fifths and fifteen

Numerical expression:

Solution:

Solution:
2. Write at least 2 numerical expressions for each phrase below. Then, solve.
a. Two thirds of eight
b. One sixth of the product of four and nine
3. Use $<,>$, or = to make true number sentences without calculating. Explain your thinking.
a. $217 \times\left(42+\frac{48}{5}\right)$


$$
(217 \times 42)+\frac{48}{5}
$$

b.
$\left(687 \times \frac{3}{16}\right) \times \frac{7}{12}$

$\left(687 \times \frac{3}{16}\right) \times \frac{3}{12}$
c.

$5 \times 6.99$

Name $\qquad$ Date $\qquad$

1. Use the RDW process to solve the word problems below.
a. Julia completes her homework in an hour. She spends $\frac{7}{12}$ of the time doing her math homework and $\frac{1}{6}$ of the time practicing her spelling words. The rest of the time she spends reading. How many minutes does Julia spend reading?
b. Fred has 36 marbles. Elise has $\frac{8}{9}$ as many marbles as Fred. Annika has $\frac{3}{4}$ as many marbles as Elise. How many marbles does Annika have?
2. Write and solve a word problem that might be solved using the expressions in the chart below.

| Expression | Word Problem |  |
| :---: | :---: | :---: |
| $\frac{2}{3} \times 18$ |  |  |
| $(26+34) \times \frac{5}{6}$ |  |  |
| $7-\left(\frac{5}{12}+\frac{1}{2}\right)$ |  |  |

Name $\qquad$ Date $\qquad$

1. Answer the following questions about fluency.
a. What does being fluent with a math skill mean to you?
b. Why is fluency with certain math skills important?
c. With which math skills do you think you should be fluent?
d. With which math skills do you feel most fluent? Least fluent?
e. How can you continue to improve your fluency?
2. Use the chart below to list skills from today's activities with which you are fluent.

| Fluent Skills |
| :--- | :--- |
|  |
|  |
|  |

3. Use the chart below to list skills we practiced today with which you are less fluent.

| Skills to Practice More |
| :--- |
|  |
|  |
|  |



Lesson 31: Explore the Fibonacci sequence.

Name $\qquad$ Date $\qquad$

1. Ashley decides to save money, but she wants to build it up over a year. She starts with $\$ 1.00$ and adds 1 more dollar each week. Complete the table to show how much she will have saved after a year.

| Week | Add | Total |
| :---: | :---: | :---: |
| 1 | \$1.00 | \$1.00 |
| 2 | \$2.00 | \$3.00 |
| 3 | \$3.00 | \$6.00 |
| 4 | \$4.00 | \$10.00 |
| 5 |  |  |
| 6 |  |  |
| 7 |  |  |
| 8 |  |  |
| 9 |  |  |
| 10 |  |  |
| 11 |  |  |
| 12 |  |  |
| 13 |  |  |
| 14 |  |  |
| 15 |  |  |
| 16 |  |  |
| 17 |  |  |
| 18 |  |  |
| 19 |  |  |
| 20 |  |  |
| 21 |  |  |
| 22 |  |  |
| 23 |  |  |
| 24 |  |  |
| 25 |  |  |
| 26 |  |  |


| Week | Add | Total |
| :---: | :---: | :---: |
| 27 |  |  |
| 28 |  |  |
| 29 |  |  |
| 30 |  |  |
| 31 |  |  |
| 32 |  |  |
| 33 |  |  |
| 34 |  |  |
| 35 |  |  |
| 36 |  |  |
| 37 |  |  |
| 38 |  |  |
| 39 |  |  |
| 40 |  |  |
| 41 |  |  |
| 42 |  |  |
| 43 |  |  |
| 44 |  |  |
| 45 |  |  |
| 46 |  |  |
| 47 |  |  |
| 48 |  |  |
| 49 |  |  |
| 50 |  |  |
| 51 |  |  |
| 52 |  |  |

2. Carly wants to save money, too, but she has to start with the smaller denomination of quarters. Complete the second chart to show how much she will have saved by the end of the year if she adds a quarter more each week. Try it yourself, if you can and want to!

| Week | Add | Total | Week | Add | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | \$0.25 | \$0.25 | 27 |  |  |
| 2 | \$0.50 | \$0.75 | 28 |  |  |
| 3 | \$0.75 | \$1.50 | 29 |  |  |
| 4 | \$1.00 | \$2.50 | 30 |  |  |
| 5 |  |  | 31 |  |  |
| 6 |  |  | 32 |  |  |
| 7 |  |  | 33 |  |  |
| 8 |  |  | 34 |  |  |
| 9 |  |  | 35 |  |  |
| 10 |  |  | 36 |  |  |
| 11 |  |  | 37 |  |  |
| 12 |  |  | 38 |  |  |
| 13 |  |  | 39 |  |  |
| 14 |  |  | 40 |  |  |
| 15 |  |  | 41 |  |  |
| 16 |  |  | 42 |  |  |
| 17 |  |  | 43 |  |  |
| 18 |  |  | 44 |  |  |
| 19 |  |  | 45 |  |  |
| 20 |  |  | 46 |  |  |
| 21 |  |  | 47 |  |  |
| 22 |  |  | 48 |  |  |
| 23 |  |  | 49 |  |  |
| 24 |  |  | 50 |  |  |
| 25 |  |  | 51 |  |  |
| 26 |  |  | 52 |  |  |

Lesson 32:
3. David decides he wants to save even more money than Ashley did. He does so by adding the next Fibonacci number instead of adding $\$ 1.00$ each week. Use your calculator to fill in the chart and find out how much money he will have saved by the end of the year. Is this realistic for most people? Explain your answer.

| Week | Add | Total | Week | Add | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | \$1 | \$1 | 27 |  |  |
| 2 | \$1 | \$2 | 28 |  |  |
| 3 | \$2 | \$4 | 29 |  |  |
| 4 | \$3 | \$7 | 30 |  |  |
| 5 | \$5 | \$12 | 31 |  |  |
| 6 | \$8 | \$20 | 32 |  |  |
| 7 |  |  | 33 |  |  |
| 8 |  |  | 34 |  |  |
| 9 |  |  | 35 |  |  |
| 10 |  |  | 36 |  |  |
| 11 |  |  | 37 |  |  |
| 12 |  |  | 38 |  |  |
| 13 |  |  | 39 |  |  |
| 14 |  |  | 40 |  |  |
| 15 |  |  | 41 |  |  |
| 16 |  |  | 42 |  |  |
| 17 |  |  | 43 |  |  |
| 18 |  |  | 44 |  |  |
| 19 |  |  | 45 |  |  |
| 20 |  |  | 46 |  |  |
| 21 |  |  | 47 |  |  |
| 22 |  |  | 48 |  |  |
| 23 |  |  | 49 |  |  |
| 24 |  |  | 50 |  |  |
| 25 |  |  | 51 |  |  |
| 26 |  |  | 52 |  |  |

Lesson 32:

Name $\qquad$ Date $\qquad$

Record the dimensions of your boxes and lid below. Explain your reasoning for the dimensions you chose for Box 2 and the lid.

BOX 1 (Can hold Box 2 inside.)

The dimensions of Box 1 are $\qquad$ $\times$ $\qquad$ $\times$ $\qquad$ .

Its volume is $\qquad$ .

BOX 2 (Fits inside of Box 1.)

The dimensions of Box 2 are $\qquad$ $\times$ $\qquad$ $\times$ $\qquad$ .

Reasoning:

LID (Fits snugly over Box 1 to protect the contents.)

The dimensions of the lid are $\qquad$ $\times$ $\qquad$ $\times$ $\qquad$ .

## Reasoning:

1. What steps did you take to determine the dimensions of the lid?
2. Find the volume of Box 2. Then, find the difference in the volumes of Boxes 1 and 2 .
3. Imagine Box 3 is created such that each dimension is 1 cm less than that of Box 2 . What would the volume of Box 3 be?

Name
Date $\qquad$
I reviewed $\qquad$ 's work.

Use the chart below to evaluate your friend's two boxes and lid. Measure and record the dimensions, and calculate the box volumes. Then, assess suitability, and suggest improvements in the adjacent columns.

| Dimensions and Volume | Is the Box or Lid Suitable? Explain. | Suggestions for Improvement |
| :--- | :--- | :--- |
| BOX 1 dimensions: |  |  |
| Total volume: |  |  |
| BOX 2 dimensions: |  |  |
| Total volume: |  |  |
| LID dimensions: |  |  |

Video tutorials: http://embarc.online Info for parents: http://bit.ly/pusdmath


[^0]:    unlabeled coordinate plane

